

1. Recall problems INDEPENDENT SET (IS) and VERTEX COVER (VC) from last time. Suppose that the *parameter* of both problems is the solution size. Formally, we have defined problems INDEPENDENT SET *parameterized by solution size  $k$*  and VERTEX COVER *parameterized by solution size  $k$*  but I will always omit the part after the “parameterized” if what I mean is clear from the context.

On the lecture (I hope) you saw that VC is in FPT and IS is W[1]-hard. This indicates that IS is probably not in FPT. But we have seen a polynomial reduction from IS to VC. You can trust me that a polynomial reduction is a FPT reduction. Should this not mean that IS is also in FPT? Discuss.

2. In the POINT LINE COVER problem, we are given a set of  $n$  points in the plane and an integer  $k$ . The goal is to check if there exists a set of  $k$  lines on the plane that contain all the input points. Show a kernel for this problem with  $\mathcal{O}(k^2)$  points.
3. Show that CLIQUE and INDEPENDENT SET, parameterized by the solution size  $k$ , are FPT on  $r$ -regular graphs for every fixed integer  $r$ .  $r$  being a fixed constant means that we can assume  $r \in \mathcal{O}(1)$ .

Also show that these problems are FPT with combined parameters  $k+r$ . Meaning that  $r$  is not a constant anymore and we need to consider it in the running time of the algorithm.

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Homework should start next week :)