From now until forever we denote $[a,b] = \{c \in \mathbb{Z} \mid a \le c \le b\}$, and [a] = [1,a].

- 1. In the d-HITTING SET problem, we are given a ground set U = [n], m subsets $S = \{S_i\}_{i=1}^m$ where $S_i \subseteq U$ and $|S_i| = d$, and an integer k. The goal is to find $X \subseteq U$ of size at most k such that $X \cap S_i \neq \emptyset$ for every $i \in [m]$.
 - Obtain an algorithm for 3-HITTING SET running in time $\mathcal{O}^*(3^k)$ using iterative compression.
- 2. Obtain an algorithm for d-HITTING SET running in time $\mathcal{O}^*(d^k)$ using iterative compression.
- 3. An undirected graph G is called *perfect* if for every induced subgraph H of G, the size of the largest clique in H is the same as the chromatic number of H. We consider the ODD CYCLE TRANSVERSAL PROBLEM, restricted to perfect graphs. Show an algorithm with running time $\mathcal{O}^*(2^k)$ based on iterative compression.
- 4. A graph G is a split graph if V(G) can be partitioned into sets C and I such that C is a clique and I is an independent set. In SPLIT VERTEX DELETION problem, given a graph G and an integer k, the task is to check if one can delete at most k vertices from G to obtain a split graph.
 - Provide a $\mathcal{O}^*(2^k)$ algorithm for the problem using iterative compression.
- 5*. In the CLUSTER VERTEX DELETION problem, we are given a graph G and an integer k, and the task is to find a set X of at most k vertices of G such that G X is a cluster graph (a disjoint union of cliques). Using iterative compression, obtain an algorithm for CLUSTER VERTEX DELETION running in time $\mathcal{O}^*(2^k)$.